



Breaking MPC Wallets and Digital Custodians for \$BILLION\$ Profit verichains.io/tsshock

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What is this talk about?

Private-key extraction attacks in popular GG18/GG20 based Threshold Signature Scheme (TSS) implementations, a Multi-Party Computation (MPC) protocol.



Multi Party Computation

• Joint Computation with **Private inputs**

• Private inputs are **never** revealed/computed

• Accurately calculate the result





Threshold Signature Scheme

- Joint Computation of Digital Signatures with Private shares
- Private key is split into multiple key shares
- Private key is never reconstructed by any party
- Threshold t/n party to produce the signature





GG18/GG20 protocols

- TSS for ECDSA
- Well known in the industry
- Multiple revisions
- Open-sourced implementations
- Being widely used in production



GG18/GG20 protocols





Signing ceremony

Alice

NOT REQUIRED TO UNDERSTAND MtA sub-protocols NOT REQUIRED TO UNDERSTAND



Bob



MtA sub-protocol



All inputs and outputs are sensitive data

This protocol requires a range proof!



Range proof used in MtA sub-protocol



During Signing phase $z_{A} = h_{1B}^{a} \cdot h_{2B}^{\rho_{A}} \mod \widetilde{N_{B}}$ $z_{B} = h_{1A}^{b} \cdot h_{2A}^{\rho_{B}} \mod \widetilde{N_{A}}$



Range proof used in MtA sub-protocol



Alice receives
$$z = h_1^x \cdot h_2^\rho \mod \widetilde{N}$$

x is private value of the other party

 ρ is random nonce of the other party

x should not be revealed



Range proof used in MtA sub-protocol

AliceAlice receives $z = h_1^x \cdot h_2^\rho \mod \widetilde{N}$ h_1 is in the multiplicative subgroup generated by h_2 \widetilde{N}, h_1, h_2 $h_1 = h_2^e \Rightarrow z = h_2^{ex+\rho} \mod \widetilde{N}$

x is not revealed when ρ is big enough

Requires a proof of knowledge of $\log_{h_2} h_1 \mod \widetilde{N}$

Using dlnproof of $\log_{h_2} h_1 \mod \widetilde{N}$



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dInproof



$$\tau = \rho + c \cdot \log_{h_2} h_1 \mod \phi(\tilde{N})$$

Accepts if $h_2^{\tau} = \alpha \cdot h_1^c \mod \widetilde{N}$

Repeats at least 80 times

Apply Fiat-Shamir heuristics with $c = H(\tilde{N}, h_1, h_2, \{\alpha_i\})$



GG18/GG20 protocols



TSSHOCK Attacks

Implementation weaknesses found in dInproof allows forging proofs

α-shuffleAttacks c-splitc-guess

All attacks can recover private key

Most implementations

- Single malicious party member
- Protocol seamlessly continues with no abort on attack

Many implementations, including de-facto opensource TSS frameworks in Golang and Rust found to be vulnerable. Widely used in

MPC Wallet Asset Custodian Decentralized Bridge

```
for i := range in values {
   data = append(data, values[i])
   data = append(data, delimiter)
}
```



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```





Take a guess on how many bits of 0 and 1

Prepare α for c = 1 and c = 0



Algorithm 1 α-shuffle dlnproof forging

Input: g, N.

Output: h, dlnproof for $\log_g h \mod N$.

- 1. Let $\tau = \operatorname{rand}(\mathbb{Z}_{\operatorname{ord}(g)})$. Let $\alpha = g^{\tau} \mod N$. Set all $\tau_i = \tau$.
- 2. Let $a = bytes(\alpha)$. Let $\beta = int(a|D|a)$.

3. Set
$$h = \frac{\alpha}{\beta} \mod N$$
 (so that $\beta = \frac{g^{\tau}}{h} \mod N$).

4. For *l* in
$$\{0, 1, 2, ..., \lambda\}$$
:

- (a) Temporarily set $\alpha_i = \begin{cases} \alpha & (1 \le i \le l) \\ \beta & (l+1 \le i \le \lambda) \end{cases}$ (assign α to l first α_i and β to the remaining).
- (b) Let $c_1, c_2, ..., c_{\lambda} = H(g, h, N, \alpha_1, \alpha_2, ..., \alpha_{\lambda}).$

(c) If
$$\sum c_i = \lambda - l$$
 (there are *l* challenge bits equal to
0), set $\alpha_i = \begin{cases} \alpha & (c_i = 0) \\ \beta & (c_i = 1) \end{cases}$ and return.

5. Go back to step 1.









Problem: Use a larger challenge space with no dlnproof iteration



c-split



$$\tau = \rho + c \cdot \log_{h_2} h_1 \mod \phi(\widetilde{N})$$

Accepts if $h_2^{\tau} = \alpha \cdot h_1^c \mod \widetilde{N}$

No iteration

Apply Fiat-Shamir heuristics with $c = H(\tilde{N}, h_1, h_2, \{\alpha_i\})$



c-split

$$\tau = \rho + c \cdot \log_{h_2} h_1 \mod \phi(\widetilde{N})$$

If $\log_{h_2} h_1 = \frac{1}{2}$ and c is an even number, τ exists, proof exists
If $\log_{h_2} h_1 = \frac{1}{e}$ and c divides e, τ exists, proof exists
It should be noted that $\frac{1}{e}$ is non-existent in group $\phi(\widetilde{N})$ if $gcd(e, \phi(\widetilde{N})) \neq 1$
But if c divides e , the proof can be calculated

Probability for a random *c* divides *e* is $\frac{1}{e} \rightarrow$ Brute force *c*



c-split

Using brute force so *e* should be small 30-50 bits (computing power)

Private inputs extracted are in *mod* e

e is small so the value cannot be fully extracted from 1 signature

Acquire more signature(s) and use lattice attack* to recover full value

*Similar to nonce leakage attack on ECDSA





Problem: Reduction of dlnproof iterations





$$\tau = \rho + c \cdot \log_{h_2} h_1 \mod \phi(\widetilde{N})$$

Accepts if $h_2^{\tau} = \alpha \cdot h_1^c \mod \widetilde{N}$

Repeat fewer times

Apply Fiat-Shamir heuristics with $c = H(\tilde{N}, h_1, h_2, \{\alpha_i\})$





Predictable challenge is insecure

Low rounds number can be brute force for all challenge bits

Probability for a successful guess is $\frac{1}{2^{iterations}}$



Recap attacks

Bug	Attack	Why?
Ambiguous encoding scheme	α -shuffle	Same encoding for different integer lists
Reduction of dInproof iterations	c-guess	Easily guess challenge bits for a small number of iterations
Use a larger challenge space with no dlnproof iterations	c-split	Optimize the scheme without proving its soundness error is negligible



Affected Vendors/Libraries

Implementations	Attack Technique	PoC	Required number of		
· · · · · · · · · · · · · · · · · · ·			Malicious parties	(Re)sharing ceremonies	Signing ceremonies
Axelar (tofn)	c-split	YES	1	1	2
Binance/BNBChain (tss-lib)	α-shuffle	YES	1	1	1
ING Bank (threshold-signatures)	c-split	YES	1	1	2
Keep Network/Threshold Network	a-shuffle	YES	1	1	1
Multichain (fastMPC)	a-shuffle	YES	1	1	1
	c-guess	YES	1	1	1
Swingby (tss-lib)	a-shuffle	YES	1	1	1
Taurus (multi-party-sig)	α-shuffle	YES	1	1.5526	1
Thorchain (tss-lib)	α-shuffle	YES	1	1	1
ZenGo X (multi-party-ecdsa)	c-split	YES	2	1	1



DEMO





THORChain mainnet halted globally after our report.

Our PoC exploit could steal all assets from THORChain's vaults (US\$180M TVL) via a single malicious node.





 \$ ~
 BTC \$29,614
 ETH \$1,861
 BNB \$243
 XRP \$0.64
 ADA \$0.300
 USDC \$1.00
 USDT \$

MAR 28, 2023



THORChain mainnet halted amid new vulnerability reports

THORChain has once again halted its network, taking action as a precautionary measure while verifying reports on a potential network vulnerability.

Cross-chain liquidity protocol THORChain has paused its network due to new claims of a potential network vulnerability.

THORChain took to Twitter on March 28 to announce it has halted all trading amid reports of a potential vulnerability with a THORChain dependency that may affect the network. The decision was taken as a precautionary measure while the reports are verified, THORChain said.

The announcement came soon after social media reports indicated THORChain's liquidity platform Nine Realms and the dedicated security team THORSec received "credible reports" of a potential vulnerability affecting THORChain. The THORChain network has reportedly been subsequently halted globally.

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Conclusions

- Implement new and complex cryptography protocols can be extremely challenging and dangerous.
- Optimizations for cryptographic protocols can be also extremely challenging and dangerous.
- New cryptographic protocols must undergo a rigorous security evaluation before widely used in production.
- MPC/TSS is pretty new and has not been standardized yet.
 - prone to new vulnerabilities.
 - gradually more secure by being battle-tested and challenged by new attacks







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